

# Model to determine recrystallization temperature of tungsten based dilute solid solution alloys

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**Abstract** A new model is developed and used to predict the effect of the deformation history and the chemical purity on the recrystallization temperature of tungsten based dilute solid solution alloys.

Experience shows that incomplete recrystallization often proves to be of better use to achieve the desired balance in material properties [1]. If the recrystallization temperatures ( $T_{re}$ ) of materials, especially high temperature materials, are well known, the material properties can be well improved by controlling recrystallization during application.  $T_{re}$  of materials depends mainly on the deformation history and the chemical purity. However, the most researches are at qualitative stage at present, especially for metal alloys. In this paper, a model is developed by the thermal fluctuation model of nucleation to describe the effect of the deformation history and the chemical purity on  $T_{re}$  of dilute solid solution tungsten alloys.

The nucleation and growth process of recrystallization can be described by the nucleation theory. Time for 50% static recrystallization ( $t_{0.5}$ ) is temperature dependent and is often found to obey an Arrhenius type relationship of the form [2–4]:

$$t_{0.5}^{-1} = A \exp\left(\frac{Q}{RT_{re}}\right) \quad (1)$$

where  $Q$  is the activation energy (J/mol);  $R$  is a gas constant (J/mol K);  $T_{re}$  is the recrystallization temperature (K);  $A$  is a constant related to the initial grain size.

The time ( $t_{0.5}$ ) for static recrystallization is also commonly described by strain dependent and obeys the following form [4–7]:

$$t_{0.5} \propto \varepsilon^n \quad (2)$$

where  $n$  is a constant.

Therefore,  $T_{re}$  can be expressed as

$$\frac{1}{T_{re}} = \frac{R}{Q} n \ln \varepsilon + \frac{R}{Q} \ln B \quad (3)$$

In order to describe the relationship between the  $T_{re}$  and solute content, Gao and Zee [8] conclusions about the creep activation energy for tungsten and molybdenum based solid solution alloys were referred. The static recrystallization activation energy is assumed to be a function of atomic mismatch ( $e$ ) and solute content ( $x$ ):

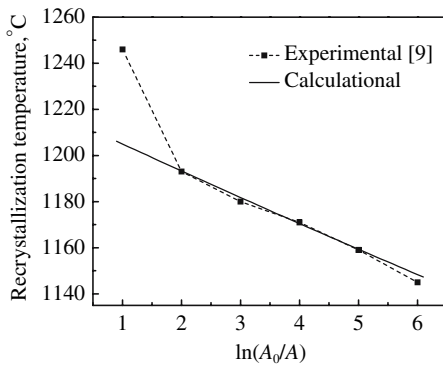
$$Q = f(e, x) = Cex^{1/2} + Q_o \quad (4)$$

$$e = |r_W - r_{solute}|/r_W \quad (5)$$

where  $e$  is the atomic mismatch;  $x$  is the molar fraction of solute atoms;  $C$  is a constant (J/mol);  $Q_o$  is the activation energy of pure tungsten;  $r_W$  and  $r_{solute}$  are the atomic radius of tungsten and solute atoms, respectively.

The relationship between strain and  $T_{re}$  of pure tungsten (the experimental data come from [9]) is shown in Fig. 1.  $T_{re}$  decreases with increasing strain. The value of the activation energy of pure tungsten is computed to be about  $Q_o=362.5$  kJ/mol.

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**Fig. 1** Relationship between  $T_{re}$  and strain

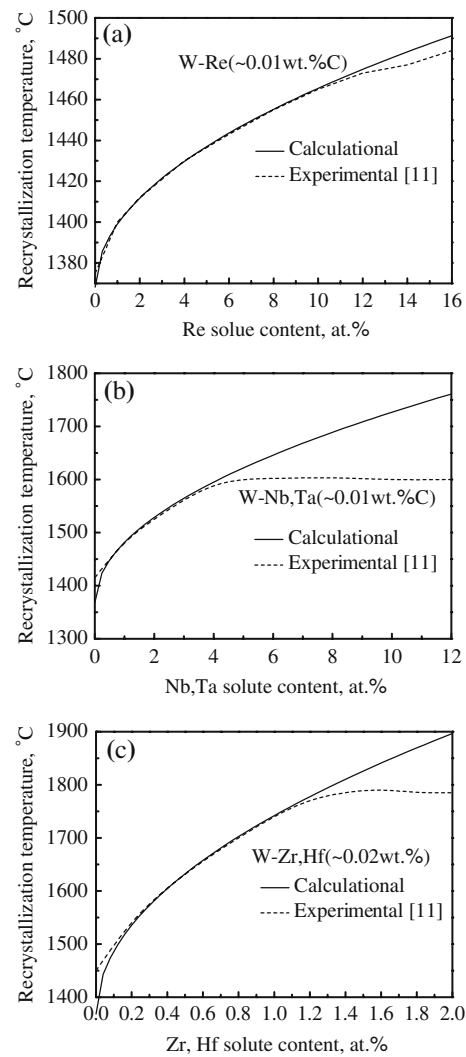
The elements of solid solution strengthened tungsten are mainly Re (Mo), Nb, Ta, Hf, Zr. The values of the atomic size mismatch between tungsten and solute atoms are given in Table 1.

As well known, recrystallization process in the metals or alloys after large deformation (generally,  $\epsilon > 0.7$ ) has completed more than 95% within a specified time (1–3 h) at an approximate minimum temperature, and the lowest temperature is defined as  $T_{re}$  [10]. The effect of solute content on  $T_{re}$  of tungsten alloys (the experimental data come from [11]) is shown in Fig. 2.  $T_{re}$  increases with increasing solute content. The calculated results compare well with the experimental results for W–Re alloys. The model predicts well when the solute content is less than 5 at.% for W–Nb alloys and less than 1.5 at.% for W–Zr alloys. However, the calculated results are much higher than the experimental results with increasing solute content.

The vast majority of structural transformations in materials take place by the mechanism of “nucleation and growth”. The nucleation and growth for recrystallization is completed by the movement of the thermally activated atoms. The addition of the solute hinders the movement thus imposing an extra energy barrier in these tungsten based solid solution alloys, and the larger the atomic size mismatch is, the stronger the barrier is, indicating that the additional energy is required. Therefore,  $T_{re}$  and activation energy increase with increasing solute content and the atomic size mismatch. The effect of solute content on the activa-

**Table 1** Atomic size mismatch between tungsten and some types of solutes [8]

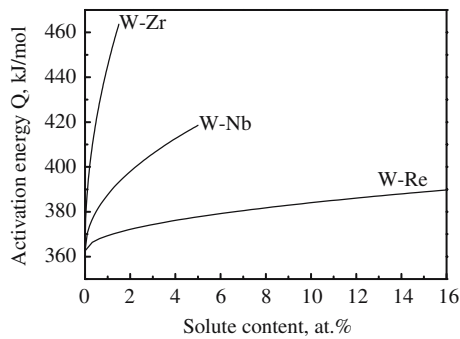
Elements	Atomic radius $r$ (nm)	Atomic size mismatch $e$
W	0.138	0.000
Re(Mo)	0.134	0.029
Nb(Ta)	0.144	0.043
Hf(Zr)	0.155	0.123



**Fig. 2** Effect of solute content on  $T_{re}$  of tungsten Alloys ( $\epsilon=0.7$ ). (a) Re; (b) Nb (Ta); (c) Zr (Hf)

tion energy is shown in Fig. 3. The activation energy is between 360–390 kJ/mol for W–Re alloys, which is a little lower than the creep activation energy for W–Re alloys [12], indicating that the recrystallization process is a thermally activated process and a part energy was reserved after cold working. However, no data for W–Zr and W–Nb alloys are available.

With increasing solute content, the barriers to recrystallization nucleation and growth are increased, and the recrystallization temperature of tungsten alloys should also increase. However, the calculated results gradually deviate from the experiment results at high solute levels. Firstly, the melting point of tungsten alloys are abruptly decreased as the solute contents (especially for Zr, Hf, Nb, Ta) reach to certain level [11], and the solubility of the solid solute atoms in tungsten is decreased, in other words, the effect of solid



**Fig. 3** Relationship between the activation energy and solute content

solution strengthening on tungsten alloys is weakened at high solute levels; on the other hand, the higher flow stress levels occur as solute levels are raised, which tend to counteract increases in barriers to recrystallization nucleation and growth, and the stored energy in tungsten alloys is increased. Therefore, there occurs a leveling off at high solute levels in the plots of the recrystallization temperature against the solute contents, and the calculated results by the model are higher than the experimental results.

In conclusion, we describe here a new model which has proved to provide very reasonable predictions for the effect of solute content and strain on the recrystallization

temperature of dilute solid solution tungsten alloys. The model successfully explains the available data in tungsten based dilute solid solution alloys.

## References

1. Smid I, Akiba M, Vieider G, Plöchl L (1998) *J Nucl Mater* 160:258
2. García-Mateo C, López B, Rodríguez-Ibabe JM (2000) *Scripta Metall* 42:137
3. Medina SF (1995) *Scripta Metall* 32:43
4. Waryoba DR (2003) Deformation and annealing behavior of heavily drawn oxygen free high conductivity (OFHC) Copper. A Doctoral Degree Dissertation in the Florida State University, p 261
5. Hodgson PD, Brownrigg A, Algie SH In: Chandra T (ed) *Recrystallization '90*, ed., p. 541, TMMMS, Warrendale, PA
6. Sellars CM (1985) *Czech J Phys* 35:239
7. Barnett MR, Kelly GL, Hodgson PD (2000) *Scripta Metall* 43:365
8. Gao H, Zee R, (1995) *Scripta Metall* 32:1665
9. Davis JW, Barabash VR, Makhankov A, Ploch L, Slattery KT (1998) *J Nucl Mater* 258–263:308
10. Gorelik SS, (1981). *Recrystallization in metals and alloys*. MIR Publishers, Moscow. Translated from the Russian by V. Afanasyev, J. M. Tong. Mechanical Industry Press, Beijing, 1985, p 331 (in Chinese)
11. Makarov P, Povarova K, (2002) *Int J Refr Met Hard Mater* 20:277
12. Ramalingam ML, Jacobson DL (1986) *J Less-common Met* 123:153